

21.5/25 (col) 20

EE345 - Introduction to Microcontrollers

Exam 2

27th Nov. 2016 B

Student Name: یزن نضال حسن زاید

Student No.: 20150024033

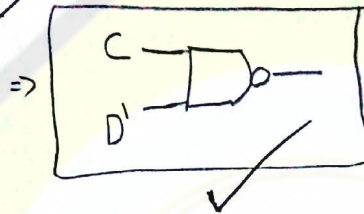
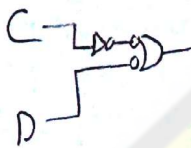
Problem 1 (5 points)

Simplify the following function, and implement it with NAND gates:

$$F(A, B, C, D) = AC'D' + A'D + ABD + AB'D + A'C'D'$$

5

$$F = C' + D$$



AB \ CD	00	01	11	10
00	1	1	1	1
01	1	1	1	1
11	1	1	1	1
10	1	1	1	1

Problem 2 (6 points)

With the use of maps, find the simplest sum-of-products form of the function $F = fg$, where

$$f = (a + c + d)(b + c + d)(c' + d')(a' + b' + c') \quad f' = a'c'd' + b'c'd' + cd + abc$$

$$g = a'c' + c'd' + b'd' + acd + bcd$$

2.5

ab \ cd	00	01	11	10
00	1	1	1	1
01	1	1	1	1
11	1	1	1	1
10	1	1	1	1

$$f' = cd' + a'c'd' ?$$

≠

F map?

ab \ cd	00	01	11	10
00	1	1	1	1
01	1	1	1	1
11	1	1	1	1
10	1	1	1	1

$$g = b'd' +$$

Problem 3 (8 points)

Design a combinational circuit with three inputs, x , y , and z , and three outputs, A , B , and C . When the binary input is 0, 1, 2, or 3, the binary output is two greater than the input. When the binary input is 4, 5, 6, or 7, the binary output is three less than the input.

inputs				outputs			
	x	y	z	A	B	C	
0	0	0	0	0	1	0	$0+2$
1	0	0	1	0	1	1	$1+2$
2	0	1	0	1	0	0	$2+2$
3	0	1	1	1	0	1	$3+2$
4	1	0	0	0	0	1	$4-3$
5	1	0	1	0	1	0	$5-3$
6	1	1	0	0	1	1	$6-3$
7	1	1	1	1	0	0	$7-3$

$x \backslash yz$	00	01	11	10
0			1	1
1			1	

$$A = x'y + yz = y(x' + z)$$

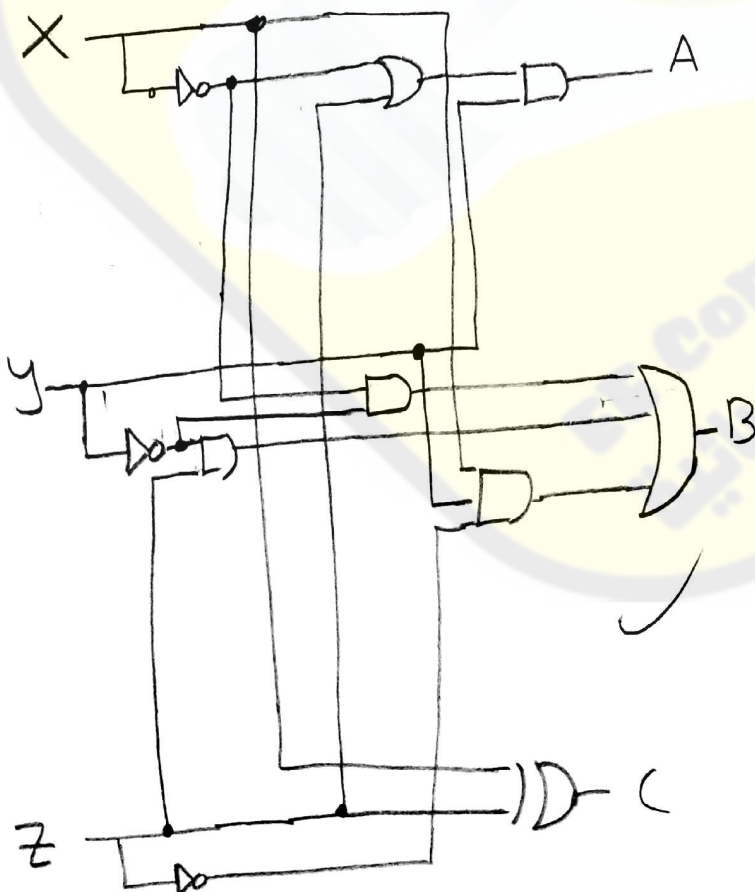
$x \backslash yz$	00	01	11	10
0	1	1		
1		1		1

$$B = y'z + x'y' + xy'z'$$

$x \backslash yz$	00	01	11	10
0		1	1	
1	1	1		1

$$C = x'z + xz'$$

$$C = x \oplus z$$



Problem 4 (6 points)

A sequential circuit has two JK flip-flops A and B and one input x. The circuit is described by the following flip-flop input equations:

$$J_A = x \quad K_A = B' \quad J_B = x \quad K_B = A$$

(a) Derive the state equations $A(t+1)$ and $B(t+1)$ by substituting the input equations for the J and K variables.

(b) Write down the state table and draw the state diagram of the circuit.

⇒ Characteristic Equation:

$$Q(t+1) = JQ' + K'Q$$

$$\Rightarrow A(t+1) = \underset{\substack{\downarrow \\ x}}{J_A} A' + \underset{\substack{\downarrow \\ (B')}}{K_A'} A \Rightarrow A(t+1) = xA' + AB$$

$$\Rightarrow B(t+1) = \underset{\substack{\downarrow \\ x}}{J_B} B' + \underset{\substack{\downarrow \\ A'}}{K_B'} B \Rightarrow B(t+1) = xB' + A'B$$

Present state		input x	Next state	
A	B		A	B
0	0	0	0	0
0	0	1	1	1
0	1	0	0	1
0	1	1	1	1
1	0	0	0	0
1	0	1	0	1
1	1	0	1	0
1	1	1	1	0

