

Jordan University of Science and Technology,
Department of Electrical Engineering
EE305- Second Exam

1st semester 2011

Name: _____

Instructor: د. مازن الميسري

Section: 2:15 ~ 3:15

1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
B	B	C	D	D	A	C	D	C	B	D	B	D	A	B	C

✓ **Q1)** If the three data points (0,1), (1,2) and (2,8) are best fit to $e^{\beta x}$ the value of β is:
 A) 0.3567 B) 0.6931 C) 0.9704 D) 0.4951

Ⓢ **Q2)** Given the following two pieces of quadratic splines that sandwich a knot at $x=1$ as $s_{k+1}(x) = 1.5x^2 + bx + 5$ and $s_k(x) = x^2 + 2x + a$, then the values of a and b , respectively are: A) (1.5, 2.5) B) (4.5, 1) C) (3, 0) D) (6, 4)

✓ **Q3)** The element ℓ_{32} of the lower triangular matrix [L] in the [L][U] decomposition

of the matrix $\begin{bmatrix} 25 & 5 & 4 \\ 5 & 9 & 16 \\ 5 & 5 & 22 \end{bmatrix}$ is: A) 1.73 B) zero C) 0.5 D) 1.5

Q4) Consider the linear system:

$$\begin{cases} 2y + 3z = 1 \\ 2x + 5y + 2z = -2 \\ 3x + y + z = 3 \end{cases}$$

Starting with initial guess $[0, 0, 0]$ the value of x , y and z after two iterations using converging Gauss-Seidel iteration is:

A) $[1.000, -0.800, 0.867]$

B) $[1.022, -0.307, 0.600]$

C) $[1.000, -0.400, 0.333]$

D) $[0.978, -1.138, 1.092]$

For the data given below answer the following two questions:

x_i	0	1	2	3
y_i	-1	2	2	3

Q5) The intercept with y-axis of the straight line that best fit the data equals:

A) -1.1 B) -0.6 C) -0.3 D) 1.1

Q6) The coefficient of determination for the fitting in the previous problem equals:

A) 0.9500 B) 0.6889 C) 0.9222 D) 0.8000

Q7) The degree of the polynomial that passes through $n + 1$ data points equals:

B) $n + 1$ B) n C) n or less D) $n + 1$ or less

Q8) The table below shows the velocity versus time.

Time(s)	0	15	18	22	24
Velocity (m/s)	22	25	a	25	123

The velocity at $t=16$ seconds was estimated to be 30.429 m/s using quadratic interpolating polynomial. The value of a is most nearly to:

A) 35 m/s B) 36 m/s C) 37 m/s D) 35.5 m/s

Q9) The interpolation polynomial $p(x)$ of degree 3 passes through the points $(1, 1)$, $(2, -1)$, $(0, 0)$ and $(3, 2)$ (using the divided difference method) is:

A) $\frac{3}{2}x^3 - 6x^2 + \frac{11}{2}x + 1$ B) $\frac{7}{6}x^3 - 5x^2 - 1$ C) $\frac{4}{3}x^3 - \frac{11}{2}x^2 + \frac{31}{6}x$ D) $\frac{7}{3}x^3 - \frac{17}{2}x^2 + \frac{43}{6}x$

Q10) If the data given below

X_i	1	2	3
Y_i	1.5	2.5	2

are fitted to $f(x) = \sqrt{1+ax^b}$, then the values of a and b respectively are:

- A) 1.224 and -1.140 B) 1.546 and 0.934 C) 3.77 and 0.065 D) 0.572 and 0.114
-

Q11) What is $f(x_0)$ given that

$$x_0 = 0, x_1 = 0.4, x_2 = 0.7, f(x_2) = 4, f[x_2, x_1] = 10, f[x_2, x_1, x_0] = \frac{50}{7}$$

- A) 1 B) 3 C) 1.5 D) -1
-

Q12) For the following system of equations $x^2 + y^2 = 4$, $e^x + y = 1$
The value of x from the first iteration using Newton-Raphson method with initial guesses $x_0 = y_0 = 1$ is:

- A) -1.163953 B) 3.335387 C) 1.337769 D) -3.245681
-

Q13) A robot needs to follow a path that passes consecutively through six points. The shortest smooth path is obtained by:

- A) a fifth order polynomial through the data B) linear splines through the data
C) quadratic splines through the data D) a third order polynomial regression

Q14 The following data of the velocity of a body is given as a function of time.

Time (s)	0	15	18	22	24
Velocity (m/s)	12	21	36	28	123

Use 2nd order Lagrange interpolating polynomial to find the best value of the velocity at 16 seconds

- A) 27 B) 28 C) 29 D) 30

Q15 In order to interpolate n-data points using k-order spline, the number of continuity (value and derivatives) conditions one should satisfy equals:

- A) $k(n-2)$ B) $n(k-1)$ C) $(n-1)(k-2)$ D) nk

Q16 Given the linear system: $2x_1 + x_2 = 3$, $x_1 + ax_2 = b$. What values of a and b that make the system with no solution:

- A) $a=2/3$ and $b=1$ B) $a \neq 1/2$ and $b=2/3$ C) $a=1/2$ and $b \neq 2/3$ D) None

$$J = \begin{bmatrix} \frac{\partial f_1}{\partial x_1} & \frac{\partial f_1}{\partial x_2} \\ \frac{\partial f_2}{\partial x_1} & \frac{\partial f_2}{\partial x_2} \end{bmatrix}, \quad \begin{bmatrix} n & \sum x \\ \sum x & \sum x^2 \end{bmatrix} \begin{pmatrix} a_0 \\ a_1 \end{pmatrix} = \begin{pmatrix} \sum y \\ \sum xy \end{pmatrix}, \quad r^2 = \frac{S_t - S_r}{S_t} = \frac{\sum (y - \bar{y})^2 - \sum (y - y_{\text{model}})^2}{\sum (y - \bar{y})^2},$$

$$f[x_2, x_1, x_0] = \frac{f[x_2, x_1] - f[x_1, x_0]}{x_2 - x_0}, \quad P_n(x) = \sum_{k=0}^n f(x_k) L_k(x), \quad L_k(x) = \prod_{j=0, j \neq k}^n \left(\frac{x - x_j}{x_k - x_j} \right)$$