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Ch. 5 / Gases

Chem107

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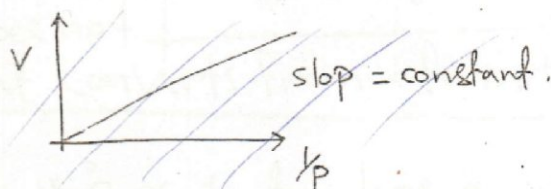
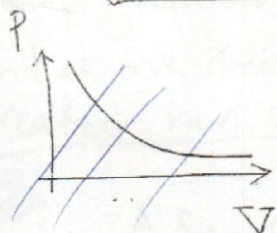
5.3 The Gas Laws:

* Boyle's Law:

pressure $\rightarrow 1 \text{ atm} = 760 \text{ mm Hg} = 760 \text{ torr} = 101325 \text{ Pa}$

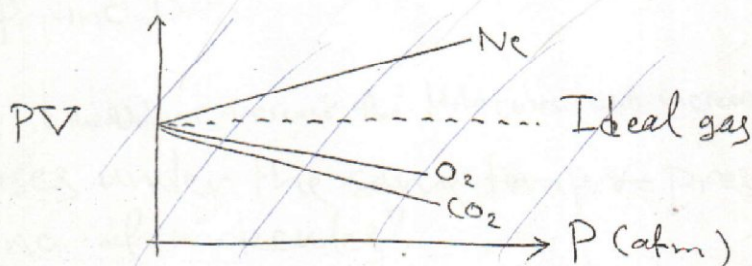
$$P \propto 1/V \Rightarrow P = \text{constant } K \Rightarrow PV = \text{constant}$$

$$P_1 V_1 = P_2 V_2 \text{ at constant temp.}$$



* Boyle's law holds precisely only at very low pressures. Measurements at higher pressures reveal that PV is not constant but varies as the pressure is varied.

- A gas that strictly obeys Boyle's law is called an ideal gas.



Ex. Consider a 1.53 L sample of SO_2 -gas at $P = 5.6 \times 10^3 \text{ Pa}$. The pressure is changed to $1.5 \times 10^4 \text{ Pa}$, at constant temp. What will be the new volume of the gas? Calculate the change of volume?

$$P_1 V_1 = P_2 V_2 \Rightarrow (5.6 \times 10^3 \text{ Pa})(1.53 \text{ L}) = (1.5 \times 10^4 \text{ Pa}) V_2$$

$$\Rightarrow V_2 = 0.57 \text{ L} \text{ which is less than } V_1 \text{ due to inc. } \uparrow \text{ in } P.$$

(SO_2) Source of acid rain, found in exhaust of vehicles

the volume is decreased by ()

$$t(^{\circ}\text{C})$$

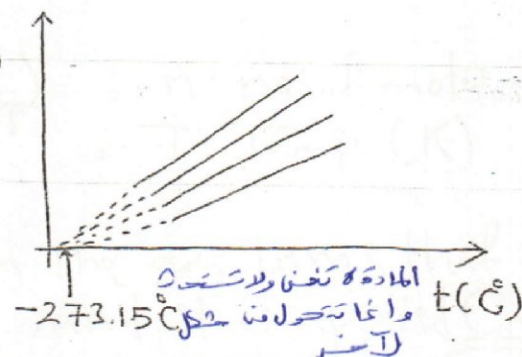
$$T(\text{K}) = t(^{\circ}\text{C}) + 273$$

* Charles's Law : (Charles's & Gay-Lussac's Law) —
(Frensh-Balloon) $V \propto T$ With a Constant Pressure

$$V = bT \Rightarrow \frac{V_1}{T_1} = \frac{V_2}{T_2}$$

b : constant

-273.15°C (Zero Kelvin = absolute Zero)
Can not be reached because at this temp. volume will be Zero and as we know matter does not created nor destroyed but converts from a form to another



Ex. A sample of gas at 15°C & 1 atm has a volume of 2.58 L. What volume will this gas occupy at 38°C & 1 atm?

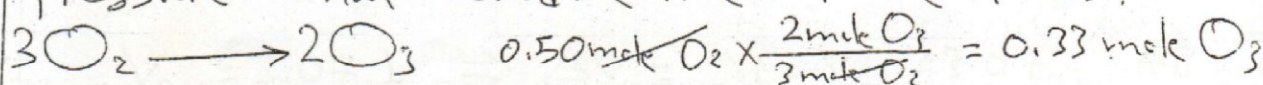
$$\frac{V_1}{T_1} = \frac{V_2}{T_2} \Rightarrow \frac{2.58\text{ L}}{288\text{ K}} = \frac{V_2}{311\text{ K}} \Rightarrow V_2 = \underline{2.79\text{ L}}$$

$V_2 > V_1$ because temp. inc. $\uparrow$.

* Avogadro's Law : if the Volume increases the Molecules will increase too
"Equal volume of gases under the same temp. & pressure contain the same no. of molecules".

$$V \propto n \Rightarrow V = bn \Rightarrow \frac{V_1}{n_1} = \frac{V_2}{n_2} \quad n: \text{no. of moles.}$$

Ex. Suppose a sample of 12.2 L contains 0.50 mole O_2 at $p = 1\text{ atm}$ $t = 25^{\circ}\text{C}$. If all O_2 is converted into Ozone O_3 at the same temp & pressure. what would be the volume of O_3 ?



$$\frac{V_1}{n_1} = \frac{V_2}{n_2} \Rightarrow \frac{12.2\text{ L}}{0.50\text{ mole}} = \frac{V_2}{0.33\text{ mole}} \Rightarrow V_2 = 8.1\text{ L}$$

$$1 \text{ atm} = 760 \text{ mm Hg} = 760 \text{ torr} = 101325 \text{ Pa}$$

5.4 The Ideal Gas Equation:

$$\Rightarrow PV = nRT$$

P: Pressure (atm) ; V: Volume (L) ; n: no. of moles
 R: gas constant = $0.0821 \text{ Latm mol}^{-1} \text{ K}^{-1}$; T: Temp. (K)
 $= 8.314 \text{ J mol}^{-1} \text{ K}^{-1}$

The previous eq. is derived from the gas laws that are mentioned in the previous sec., and it is applied Only for the ideal gases. But if the gas is real (not ideal) it can be applied under low pressure & high temp & low n

Ex. A sample of H_2 -gas has a volume = 8.56 L & $T = 0^\circ \text{C}$ with $P = 1.5 \text{ atm}$. Calculate no. of moles of H_2 .

$$PV = nRT \Rightarrow n = \frac{PV}{RT} = \frac{1.5 \text{ atm} \times 8.56 \text{ L}}{0.0821 \text{ Latm mol}^{-1} \text{ K}^{-1} \times 273 \text{ K}}$$

$$n = 0.57 \text{ moles } \text{H}_2$$

Ex. A sample of gas has $P = 345 \text{ torr}$ at $T = -15^\circ \text{C}$ & $V = 3.48 \text{ L}$. If the conditions are changed so that $T = 36^\circ \text{C}$ & $P = 468 \text{ torr}$, what will be the change in volume?

$$PV = nRT \Rightarrow \frac{PV}{T} = nR = \text{constant}$$

$$\frac{P_1 V_1}{T_1} = \frac{P_2 V_2}{T_2} \Rightarrow \frac{(345 \text{ torr})(3.48 \text{ L})}{(258 \text{ K})} = \frac{(468 \text{ torr}) V_2}{(309 \text{ K})}$$

$$V_2 = 3.07 \text{ L} \Rightarrow \Delta V = V_f - V_i = 3.07 - 3.48 = -0.41 \text{ L}$$

Volume is decreased by 0.41 L .

The density & Molar mass of the ideal gas can be calculated also from the ideal gas law:

$$PV = nRT \Rightarrow PV = \frac{m}{M} RT \Rightarrow PM = \frac{m}{V} RT$$

$$\frac{m}{V} = d = \text{density} \Rightarrow PM = dRT$$

$$d = \frac{PM}{RT} \Rightarrow M: \text{Molar mass of the ideal gas (g/mol)}$$

m : mass of the ideal gas (g)

d = density in unit of g/L

Also Molar mass: $M = \frac{dRT}{P} = \frac{9 \text{ g/L} \cdot 1 \text{ atm} \cdot 273 \text{ K}}{1 \text{ atm}} = 9 \text{ g/mol}$

ex on ideal gas at $P = 730 \text{ torr}$

$V = 350 \text{ mL}$, at 25°C has

a mass of 0.023 g

Identify the gas

Molar mass = :

1) H_2O 2) CO_2 3) N_2

$$M = \frac{\overset{\text{gram}}{m} RT}{P V} \text{ if density is unknown.}$$

$$M = \frac{dRT}{P} \text{ if density is known (1)}$$

5.5 Gas Stoichiometry:

One mole of any ideal gas at $t = 0.0^\circ\text{C}$ (273.15 K) & $P = 1 \text{ atm}$ will occupy a volume = 22.4 L.

This volume is called molar volume = $\bar{V}$, and these conditions (0°C & 1 atm) is called Standard Temp. & Pressure (STP)

$$(\bar{V})_{\text{STP}} = 22.4 \text{ L/mole. For the ideal gas.}$$

Ex. A sample of N_2 -gas has Volume = 1.75 L at STP. How many moles of N_2 are present?

$$1.75 \text{ L } \text{N}_2 \times \frac{1 \text{ mole } \text{N}_2}{22.4 \text{ L } \text{N}_2} = 7.81 \times 10^{-2} \text{ moles } \text{N}_2$$

(Calculate no. of N_2 -molecules: Ans. = 4.7×10^{22} molecules N_2)

$$7.81 \times 10^{-2} \text{ moles } \text{N}_2 \times \frac{6.023 \times 10^{23}}{1 \text{ mole } \text{N}_2} = 47.03 \times 10^{21}$$

Ex. Calculate V_{CO_2} at STP produced from the decomposition of 152g $CaCO_3$ by the following rxn.!



$$152g \text{ } CaCO_3 \times \frac{1 \text{ mole } CaCO_3}{100.09g \text{ } CaCO_3} \times \frac{1 \text{ mole } CO_2}{1 \text{ mole } CaCO_3} \times \frac{22.4L \text{ } CO_2}{1 \text{ mole } CO_2} = 34.1 L \text{ } CO_2$$

* * * Ex. A sample of methane (CH_4) has $V = 2.80L$ at $t = 25^\circ C$ & $P = 1.65 \text{ atm}$, was mixed with O_2 that has $V = 35.0L$ at $t = 31^\circ C$ & $P = 1.25 \text{ atm}$. The mixture was ignited to form CO_2 & H_2O . Calculate volume of CO_2 that is formed at $t = 125^\circ C$ & $P = 2.50 \text{ atm}$.



$$PV = nRT \Rightarrow n_{CH_4} = \frac{PV}{RT} = \frac{1.65 \text{ atm} \times 2.80 L}{0.0821 L \cdot \text{atm} / \text{mol} \cdot K \times 298 K} = 0.189 \text{ mole } CH_4$$

$$n_{O_2} = \frac{1.25 \text{ atm} \times 35.0 L}{0.0821 L \cdot \text{atm} / \text{mol} \cdot K \times 304 K} = 1.75 \text{ mole } O_2$$

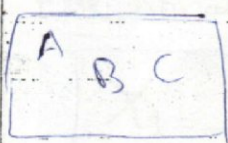
$$0.189 \text{ mole } CH_4 \times \frac{1 \text{ mole } CO_2}{1 \text{ mole } CH_4} = 0.189 \text{ mole } CO_2$$

$$PV = nRT \Rightarrow V_{CO_2} = nRT/P = \frac{0.189 \text{ mole} \times 0.0821 L \cdot \text{atm} / \text{mol} \cdot K \times 398 K}{2.50 \text{ atm}}$$

$$V_{CO_2} = 2.47 L$$

5.6. Dalton's Law of Partial Pressures:

"For a mixture of gases in a container, the total pressure exerted is the sum of the pressures that each gas would exert if it were alone"



$$P_{\text{tot}} = P_1 + P_2 + P_3 + \dots$$

P_i : Partial Pressure of gas 1

$$= \frac{n_1 RT}{V} + \frac{n_2 RT}{V} + \frac{n_3 RT}{V} + \dots = \frac{n_{\text{tot}} RT}{V} = P_{\text{tot}}$$

$P_{tot.}$ depends on the total no. of moles whatever the ideal gas (quantitative not qualitative property) (depends on amount not nature identity)

This leads to two important properties about the ideal:

- (1) The volume for particles of the ideal gas must not be important
- (2) The forces among the particles must not be important too.

Ex. 46.0 L He at $t = 25^\circ\text{C}$ & $P = 1.0 \text{ atm}$, & 12.0 L O_2 at 25°C

1 atm were pumped into a container with $V = 5.0 \text{ L}$.

Calculate the partial pressure of each gas in the container, at $t = 25^\circ\text{C}$ $P_{total}?$

$$\left(\frac{P_1 V_1}{T_1} \right)_{\text{He}} = \left(\frac{P_2 V_2}{T_2} \right)_{\text{He}} \Rightarrow \frac{1 \times 46}{298\text{K}} = \frac{P_2 \times 5}{298\text{K}} \Rightarrow P_2 = P_{\text{He}} = 9.2 \text{ atm}$$

$$\left(\frac{P_1 V_1}{T_1} \right)_{\text{O}_2} = \left(\frac{P_2 V_2}{T_2} \right)_{\text{O}_2} \Rightarrow \frac{1 \times 12}{298} = \frac{P_2 \times 5}{298} \Rightarrow P_2 = P_{\text{O}_2} = 2.4 \text{ atm}$$

$$P_{\text{tot.}} = 2.4 + 9.2 = 11.6 \text{ atm}$$

OR: $PV = nRT \Rightarrow n_{\text{He}} = PV/RT_1 = (1 \times 46)/(0.0821 \times 298) = 1.9$

$$P_2 V_2 = n_{\text{He}} R T_2 \Rightarrow P_{\text{He}} = n_{\text{He}} R T_2 / V_2 = (1.9 \times 0.0821 \times 298) / 5 = 9.2$$

$$n_{\text{O}_2} = P_1 V_1 / R T_1 = (1 \times 12) / (0.0821 \times 298) = 0.49 \text{ mole O}_2$$

$$P_{\text{O}_2} = n_{\text{O}_2} R T_2 / V_2 = (0.49 \times 0.0821 \times 298) / 5 = 2.4 \text{ atm}$$

* Mole Fraction: X_i

The ratio of no. of moles of a given component in a mixture to the no. of moles of the mixture.

$$X_1 = \frac{n_1}{n_{\text{tot.}}} = \frac{n_1}{n_1 + n_2 + \dots}$$

unitless

$$X_i = \frac{n_i}{n_1 + n_2 + \dots} = \frac{P_i(V/RT)}{P_1(V/RT) + P_2(V/RT)} = \frac{P_i}{P_1 + P_2 + \dots}$$

$$\boxed{X_i = \frac{n_i}{n_{\text{tot}}} = \frac{P_i}{P_{\text{tot}}}}$$

X is unitless

$$\begin{cases} X_1 + X_2 + X_3 = 1 \\ 0 \leq X_1 \leq 1 \\ 0 \leq X_2 \leq 1 \\ 0 \leq X_3 \leq 1 \end{cases}$$

Ex. The mole fraction of N_2 in air is 0.7808. Calculate the partial pressure of N_2 at sea level. (1 atm)
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$$X_{N_2} = 0.7808 = \frac{P_{N_2}}{P_{\text{tot}}} = \frac{P_{N_2}}{P_{\text{atm}}} = \frac{P_{N_2}}{1.0 \text{ atm}} \quad (\text{sea level } P = 1.0 \text{ atm})$$

$$\Rightarrow P_{N_2} = 0.7808 \text{ atm} = 593 \text{ torr}$$

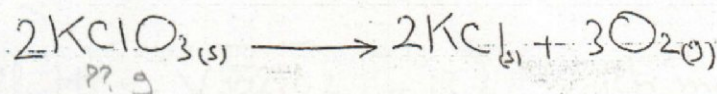
* Collection of gas over water, $\text{Mg} + \text{HCl} \rightarrow \text{MgCl}_2 + \text{H}_2$
 limit exis

In some experiments, gases are collected over water & due to water has vapor pressure, the pressure over water will be

$$\boxed{P_{\text{tot}}} = P_{H_2O} + P_{\text{gas}} \quad (\text{not the gas only over water})$$

in the container

Ex. A sample of $KClO_3$ was heated in a test tube and decomposed according to the following chemical equation:



The O_2 was collected over water at $t = 22^\circ\text{C}$ & $P_{\text{tot}} = 754 \text{ torr}$.
 $V_{O_2} = 0.650 \text{ L}$ & P_{H_2O} (vapor pressure of water) = 21.0 torr at $t = 22^\circ\text{C}$.
 Calculate required mass of $KClO_3$.

ideal gas law
 $P = \frac{nRT}{V}$

$$P_{\text{tot.}} = 754 \text{ torr} = P_{\text{H}_2\text{O}} + P_{\text{O}_2}$$

$$P_{\text{O}_2} = 754 - P_{\text{H}_2\text{O}} = 754 - 21 = 733 \text{ torr}$$

$$PV = nRT \Rightarrow n_{\text{O}_2} = \frac{PV}{RT} = \frac{(733/760) \text{ atm} \times 0.650 \text{ L}}{0.0821 \text{ L atm mol}^{-1} \text{ K}^{-1} \times 295 \text{ K}}$$

$$n_{\text{O}_2} = 2.59 \times 10^{-2} \text{ mole O}_2$$

$$2.59 \times 10^{-2} \text{ mole O}_2 \times \frac{2 \text{ mole KClO}_3}{3 \text{ mole O}_2} \times \frac{122.69 \text{ g KClO}_3}{1 \text{ mole KClO}_3} = \underline{\underline{2.12 \text{ g KClO}_3}}$$

5.7: The Kinetic Molecular Theory of Gases

Diffusion
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Diffusion: Term used to describe the mixing of gases.

Effusion: Term used to describe the process by which a gas under a pressure escapes from container to another through small opening.

Thomas Graham found experimentally that the rate of diff. of gas is inversely proportional to the square root of the mass of its particles.

$$\frac{\text{Rate of diff. of gas 1}}{\text{Rate of diff. of gas 2}} = \frac{\sqrt{M_2}}{\sqrt{M_1}} \quad (\text{Graham's Law of eff})$$

M_1 & M_2 : Molar mass of gases 1 & 2.

Ex. Calculate the ratio of diff. of H_2 to UF_6

$$\frac{\text{Rate diff. H}_2}{\text{Rate diff. UF}_6} = \frac{\sqrt{352.02}}{\sqrt{2.016}} = 13.2 \text{ which means rate of diff. of H}$$

is 13.2 times of UF_6

which one of the following statement is correct if you have 1 mole B & 2 mole A

limiting B

$$\frac{15}{17+4}$$

A) A is L.R & B excess

B) A is excess and B L.R

Which one of the following has highest rate of diffusion/effusion

- a) O_2 b) N_2 c) H_2
d) Ar e) CO_2 (Molar mass 44)

Which one of the following argument is correct in order of the dec of rate of diffusion/effusion

Calculation of diffusion of A to B

$$\frac{A}{B}$$

Which one of the following statement is correct with respect to rate of diff

of H_2 to UF_6 ?
a) rate of eff of H_2 is 13 times of UF_6

طریقه کار به این صورت

If rate of diff/eff of gas H_2 18 times gas X
Identify X

- a) CO_2
b) N_2
c) O_2
d) Ar
e) Ne

$$\frac{\text{rate H}_2}{\text{rate X}} = 18 = \sqrt{\frac{M_X}{2}}$$

$$M_X =$$

$$\frac{\text{H}_2}{X} = \frac{\sqrt{M_X}}{\sqrt{2}} = 18$$

18