

1. A vector of magnitude 10 points from the point $(5, 5\pi/4, 0)$ in cylindrical coordinates toward the origin. This vector in Cartesian coordinates is:

(a) $5\mathbf{a}_x - 5\mathbf{a}_y$ (b) $-7.07\mathbf{a}_x - 7.07\mathbf{a}_y$ (c) $5\mathbf{a}_x + 5\mathbf{a}_y$ (d) $7.07\mathbf{a}_x + 7.07\mathbf{a}_y$ (e) $10\mathbf{a}_x + 10\mathbf{a}_y$
2. The volume of the parallelepiped whose edges are the vectors \mathbf{A} , \mathbf{B} , and \mathbf{C} , is given by the magnitude of:

(a) $\mathbf{A} \cdot (\mathbf{B} \times \mathbf{C})$ (b) $\mathbf{A} \times (\mathbf{B} \times \mathbf{C})$ (c) $\mathbf{A} \times (\mathbf{B} \cdot \mathbf{C})$ (d) $\mathbf{A} \times (\mathbf{B} + \mathbf{C})$ (e) $\mathbf{A} \cdot (\mathbf{B} \cdot \mathbf{C})$
3. A charge distribution in spherical coordinates is given by $\rho_v(r) = 5re^{-2r}$ (C/m³). Using Gauss's law, the value of $\nabla \cdot (\epsilon \mathbf{E})$ at the point $(0.5, 2\pi/3, 0)$ is:

(a) $2.5e^{-1}$ (C/m²) (b) $2.5e^{-1}$ (V/m) (c) $2.5e^{-1}$ (C/m³) (d) $5e^{-1}$ (C/m²) (e) We need the value of ϵ
4. One of the following is not a property of a conservative electrostatic field:

(a) $\mathbf{E} = -\nabla V$ (b) $\nabla \times \mathbf{E} = 0$ (c) $\oint \mathbf{E} \cdot d\mathbf{l} = 0$ (d) $\int_a^b \mathbf{E} \cdot d\mathbf{l} = 0$ (e) None of these
5. When lightning occurs between the clouds themselves, or between the clouds and the earth, very large current flows through the air. This is an example of a conduction current:

(a) True (b) False
6. When a potential of 10 V is applied to a mercury column in a cylindrical container, the current is 2 A. If the mercury is now poured into another cylindrical container of twice the radius, and the same potential of 10 V is applied across its ends, what is the current now?

(a) 32 A (b) 8 A (c) 0.125 A (d) 4 A (e) 0.5 A
7. Kirchhoff's current law has its origin in the following equation:

(a) $\nabla \times \mathbf{H} = \mathbf{J}$ (b) $\nabla \cdot \mathbf{J} = 0$ (c) $\nabla \times \mathbf{E} = 0$ (d) $\nabla \cdot \mathbf{B} = 0$ (e) $\nabla \cdot \mathbf{D} = \rho_v$
8. A parallel-plate capacitor connected to a battery stores twice as much energy with a given dielectric as it does with air as dielectric. The susceptibility of the dielectric is:

(a) 0 (b) 3 (c) 2 (d) 4 (e) 1
9. If a point charge of +2 pC is brought near (but not contacting) a neutral, isolated conducting sphere of radius a , the total charge on the surface of the sphere will be:

(a) +2 pC (b) -2 pC (c) +4 pC (d) -1 pC (e) 0
10. The electric flux density at a point on the surface of a conductor is given by $\mathbf{D} = 0.2\mathbf{a}_x - 0.3\mathbf{a}_y - 0.2\mathbf{a}_z$ (pC/m²). The charge density on the surface of the conductor at the point is:

(a) 0.276 pC/m² (b) -0.325 pC/m² (c) 0.412 pC/m² (d) -0.2 pC/m² (e) -0.3 pC/m²
11. The capacitance of two conducting spherical shells of radius a in air and separated by a distance $d \gg a$, is:

(a) $2\pi\epsilon_0 a$ (b) $4\pi\epsilon_0 a$ (c) $\pi\epsilon_0 a$ (d) $8\pi\epsilon_0 a$ (e) none of these
12. When M point charges were placed between two semi-infinite conducting planes inclined to each other at an angle of 120° , the total number of charges (original+images) was 12. Therefore, M is equal to:

(a) 4 (b) 6 (c) 3 (d) 2 (e) 1
13. The two dimensional Laplace equation $V_{xx} + V_{yy} = 0$ in the region $0 \leq x \leq a$, $0 \leq y \leq b$, has a solution of the form $V(x,y) = X(x)Y(y)$ subject to the B.C.s $V(0,y) = V(a,y) = 0$. Therefore, $X(x)$ could be:

(a) $\cos(n\pi x/a)$ (b) $\sin(n\pi x/b)$ (c) $\cos(n\pi x/a)$ (d) $\sin(n\pi x/a)$ (e) $\cosh(n\pi x/a)$

14. In cylindrical coordinates, $\mathbf{B} = (2.0/\rho)\mathbf{a}_\phi$ (T). The magnetic flux that crosses the plane surface defined by $0.5 \leq \rho \leq 2.5$ m and $0 \leq z \leq 2.0$ m is:

- (a) 8 Wb (b) 6.44 Wb (c) 5.32 Wb (d) -5.32 Wb (e) 10.1 Wb

15. A current strip 2 cm wide lies in the x-y plane, and carries a current of 15 A in the \mathbf{a}_x direction. Assuming the current is uniformly distributed over the strip width and $\mathbf{B} = 0.2\mathbf{a}_y$ T, then the force on the strip per unit length is:

- (a) $-3.0\mathbf{a}_y$ N/m (b) $30\mathbf{a}_y$ N/m (c) $30\mathbf{a}_z$ N/m (d) $3.0\mathbf{a}_z$ N/m (e) $60\mathbf{a}_z$ N/m

16. Two infinite current sheets, each of constant density K_0 , are parallel and have their currents oppositely directed. The force per unit area on either sheet is:

- (a) $\mu_0 K_0^2/2$ repulsion (b) $\mu_0 K_0^2/2$ attraction (c) $\mu_0 K_0/2$ attraction (d) $2\mu_0 K_0^2$ repulsion

17. In a certain region, \mathbf{E} and \mathbf{B} fields are uniform and oriented at right angles to each other. A proton enters the region with a speed of 10^6 m/s at right angle to both fields and passes the region undeflected. If $|\mathbf{B}| = 0.5$ mT, then $|\mathbf{E}| =$:

- (a) 2 KV/m (b) 50 V/m (c) 500 V/m (d) 200 V/m (e) We need Q and m of the proton

18. The positive x-axis carries a current of $-12\mathbf{a}_x$ A. The magnetic field \mathbf{H} at the point (0, 0, -3m) is:

- (a) $(-1/\pi)\mathbf{a}_y$ (A/m) (b) $(4/\pi)\mathbf{a}_y$ (A/m) (c) $(-1/\pi)\mathbf{a}_x$ (A/m) (d) $(-2/\pi)\mathbf{a}_z$ (A/m) (e) $(3/\pi)\mathbf{a}_y$ (A/m)

19. A toroid with a mean radius of 10cm carries a current of 5A and has a turn density of 4 turns/rad. The magnetic field \mathbf{H} inside the toroid is:

- (a) 31.83 A/m (b) 200 A/m (c) 1256.6 A/m (d) 100 A/m (e) 20 A/m

20. A bar magnet is successively divided in half 10 times. At the end, how many separate magnetic dipoles do we have?

- (a) 40 (b) 0 (c) 20 (d) $(1024)^2$ (e) 1024

21. Since $\nabla \cdot \mathbf{B} = 0$, then we can write $\mathbf{B} = \nabla \times \mathbf{A}$, and therefore the magnetic flux can be written as

$$\Psi_m = \iiint (\nabla \cdot \mathbf{A}) dV.$$

- (a) True (b) False

22. One of the following is not a Maxwell equation for the static fields in a linear, homogeneous medium:

- (a) $\nabla \cdot \mathbf{H} = 0$ (b) $\nabla \times \mathbf{J} = \mathbf{H}$ (c) $\nabla \times \mathbf{D} = 0$ (d) $\oint \mathbf{B} \cdot d\mathbf{l} = \mu_0 I$ (e) $\nabla \cdot \mathbf{E} = \rho_v/\epsilon$

23. An electron is orbiting in a circular path of radius 0.5×10^{-10} m with an angular velocity of 4×10^{16} rad/s. If $|\mathbf{B}| = 0.4$ nT, what is the maximum torque on this electron?

- (a) 2×10^6 N.m (b) 5.25×10^{-16} N.m (c) 3.2×10^{-27} N.m (d) 8×10^{-26} N.m (e) 1.25×10^{-27} N.m

24. In a ferromagnetic material ($\mu = 20\mu_0$), $\mathbf{B} = 4\mathbf{a}_y$ mT. In this material, the magnetization vector \mathbf{M} is =:

- (a) $3024\mathbf{a}_y$ (A/m) (b) $3351\mathbf{a}_y$ (A/m) (c) $3.8\mathbf{a}_y$ (mA/m) (d) $3664\mathbf{a}_y$ (A/m) (e) $2414\mathbf{a}_y$ (A/m)

25. The unit of inductance is:

- (a) F/m (b) Joule/C (c) Ohm.s (d) Wb/m (e) A/s

Good Luck