

- Start each question in a new page. You HAVE to write the expressions used for calculations. If not written, you will not get any credit for that part. You HAVE to write (a), (b), (c), .... Write CLEARLY. Put the final answer in a BOX. Show your work to get partial credit. Good luck!

1. (10 points) (*Oblique Incidence*)

A uniform plane wave traveling in air is obliquely incident on the  $z=0$  interface between air and polystyrene ( $\epsilon_r=2.56$ ,  $\mu_r=1$ ). The magnetic field intensity in polystyrene is given as follows:

$$\vec{H}_2 = (-20.1824 \hat{x} + 12.614 \hat{z}) e^{-j\pi(16.96x + 27.136z)} \quad (mA/m)$$

- (3 points) Find the angle of incidence.
  - (2 points) Find the wavelength in air.
  - (5 points) Find an expression for the reflected electric field intensity  $\vec{E}_r$ . You need to substitute all needed numbers in this expression!
2. (10 points) (*Transmission Lines*)
- A  $50 \Omega$  coaxial line (with  $b/a=4.01$ ) is filled with a lossless non-magnetic dielectric. It connects a source with  $V_g=10$  V to a load  $Z_L=100 \Omega$ . The length of the transmission line is  $\ell=2.1$  meters. The magnitude of the minimum voltage along the line has been measured and found to be  $V_{min}=3.125$  V. The frequency is 300 MHz.
- (3 points) Find the input impedance  $Z_{in}$  at the beginning of the line.
  - (3 points) Find the internal impedance of the source .
  - (4 points) Now, assume that this  $50 \Omega$  coaxial line is made of copper ( $\sigma_c=5.8 \times 10^7$  S/m) and is filled with a lossy non-magnetic dielectric. Find the loss tangent (at 300 MHz) of the dielectric filling the coaxial line. (assume  $a=1$  cm).
3. (10 points) (*Here we have 3 independent short questions !!*)
- (3 points) For a short-circuited lossless  $50 \Omega$  parallel plate transmission line of length  $\ell (< \lambda/2)$ , the input admittance is  $Y_{in}=j0.058$  S. Find  $\ell$  in terms of  $\lambda$ , where  $\lambda$  is the wavelength in the transmission line.
  - (3 points) A lossless transmission line has  $Z_0=158.114 \Omega$  and  $C=40$  pF/m. It has an electrical length of  $102.458^\circ$  at 30 MHz. Find its physical length.
  - (4 points) In an oblique incidence problem, given that  $\mu_1=\mu_2$ , and  $\Gamma_{||}(\theta_i = 0) = -0.1$ . Find the incidence angle(s), if any, at which  $\Gamma_{||}=0$ ; and the incidence angle(s), if any, at which  $|\Gamma_{||}|=1$ .