

- Start each question in a new page. You HAVE to write the expressions used for calculations. Write CLEARLY. Put the final answer in a BOX. Show your work to get partial credit. Good luck!

1. (8 points) A microwave oven operating at 2.5 GHz is used to heat a piece of *chicken burger* having a complex permittivity of  $\epsilon_c = (100 - j)\epsilon_0$  (F/m). Assume that a uniform plane wave penetrates through the *burger* with an amplitude of  $E_0 = 1000$  (V/m) at its upper surface; i.e.,  $E(z=0) = 1000$  (V/m) where  $z=0$  is the upper surface of the *burger*. The thickness of this *burger* is 1 cm. (Assume  $\mu_r = 1$ )

(a) (4 points) Find the magnitude of the electric field at the bottom surface of the *burger*.

(b) (4 points) Given that the total average power dissipated inside this *burger* is 5.3 W, find its radius.

2. (7 points) A uniform plane wave traveling in a very good conductor has:

$$\vec{E} = \hat{x} 10 e^{-\alpha z} \cos(\omega t - \beta z) \text{ (V/m)}.$$

The wave goes through a phase change of 1 radian through a distance of 1.35 mm. (at a fixed time)

Also, the time-average power density at  $z=1$  cm is  $0.8221$  W/m<sup>2</sup>. Assume  $\epsilon = \epsilon_0$  and  $\mu = \mu_0$ .

Find the conductivity  $\sigma$ , the frequency, the phase velocity and the wavelength.

3. (10 points) A uniform plane wave ( $\vec{E}_i = \hat{x} E_{i0} \cos(\omega t - \beta_1 z)$  (V/m)) propagating in a non-magnetic lossless dielectric is normally incident on another lossless medium with  $\epsilon_{r2} = \mu_{r2} = 4$ . The figure below shows the standing wave in medium (1).

(a) (2 points) Find the reflection coefficient  $\Gamma$ .

(b) (2 points) Find the values of  $E_{r0}$  and  $E_{i0}$ .

(c) (3 points) Find the wavelength in medium (2).

(d) (3 points) Find the distances  $d_1$  and  $d_2$  from the interface (where  $d_1 < d_2 < \lambda_1/2$ ) at which  $|\vec{E}_1| = 8$  V/m.

