

Student Name:

Student Number:

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Note: All questions have equal marks. You must show all your work to get credit.

Problem 1(i) Determine the base b in each of the following cases:

(a) $(361)_{10} = (551)_b$

$1 \times b^0 + 5 \times b^1 + 5 \times b^2 = 361$

$5b^2 + 5b - 360 = 0$

$b^2 + b - 72 = 0 \Rightarrow (b+9)(b-8) = 0 \Rightarrow$

$b = 8$

(b) $(859)_{10} = (5B7)_b$

$7 \times b^0 + 11 \times b^1 + 5 \times b^2 = 859$

$5b^2 + 11b - 852 = 0$

$(b-12)(5b+71) = 0$

$\Rightarrow b = 12$

(ii) The following arithmetic operations are correct for one particular number system. Determine the radix for the given operations.

(a) $23 + 44 + 14 + 32 = 223$

$2b + 3 + 4b + 4 + b + 4 + 3b + 2 = 2b^2 + 2b + 3$

$10b + 13 = 2b^2 + 2b + 3$

$2b^2 - 8b - 10 = 0 \Rightarrow b^2 - 4b - 5 = 0 \Rightarrow (b-5)(b+1) = 0$

$b = 5$

$\Rightarrow \text{radix} = 5$

(b) $\text{SQRT}(51) = 6$

$\sqrt{5r+1} = 6$

$5r+1 = 36$

$5r = 35 \Rightarrow r = 7$

$\Rightarrow \text{radix} = 7$

Problem 2

(i) Using the theorems of Boolean algebra, simplify the following expression:

$f(A, B, C, D) = B + BCD + B'CD + AB + A'B + B'C$

$= B + AB + B + A'B + B + BCD + B'CD + B'C$

$= B(1+A) + B(1+A') + B(1+CD) + B'C(D+1)$

$= B + B + B + B'C$

$= B + B'C = (B+B')(B+C) = B+C$

(ii) Construct a truth table for the following function and from the truth table obtain an expression for the inverse (i.e., complement) function. Give your answer as a sum of products.

$f(A, B, C) = AC + BC + AB$

$f'(A, B, C) = A'B'C' + A'B'C + A'BC' + AB'C'$

$= A'C' + B'C' + A'B'$

A	B	C	F
0	0	0	0
0	0	1	0
0	1	0	0
0	1	1	1
1	0	0	0
1	0	1	1
1	1	0	1
1	1	1	1

Problem 3

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- (i) Expand the following Boolean function into its canonical form:

$$\begin{aligned}
 f &= B + CD + ABD' + A'B'CD' \\
 f &= (A+A')(B)(C+C')(D+D') + AB(C+C')D' + (A+A')(B+B')(CD + A'B'CD') \\
 &= ABCD + ABC'D + AB'CD + ABC'D' + A'B'CD + A'B'CD' + A'B'CD + A'B'CD' \\
 &\quad + ABC'D + ABC'D' + ABC'D + ABC'D' + A'B'CD + A'B'CD' + A'B'CD + A'B'CD' \\
 &= ABCD + ABC'D + AB'CD + ABC'D' + A'B'CD + A'B'CD' + A'B'CD + A'B'CD' \\
 &\quad + ABC'D + A'B'CD' + A'B'CD' \\
 &= \sum m(2, 3, 4, 5, 6, 7, 11, 12, 13, 14, 15)
 \end{aligned}$$

- (ii) Express the three-variable function
- $f = \sum (0, 1)$
- as a product of maxterms.

$$f(a, b, c) = \prod (2, 3, 4, 5, 6, 7)$$

$$f = (a+b+c)(a+b+c')(a'+b+c)(a'+b+c')(a'+b'+c)(a'+b'+c')$$

Problem 4

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Suppose we want to implement a circuit that has three inputs and two outputs, where:

$$f_1(A, B, C) = \sum (0, 1, 5)$$

$$f_2(A, B, C) = \sum (3, 5, 7)$$

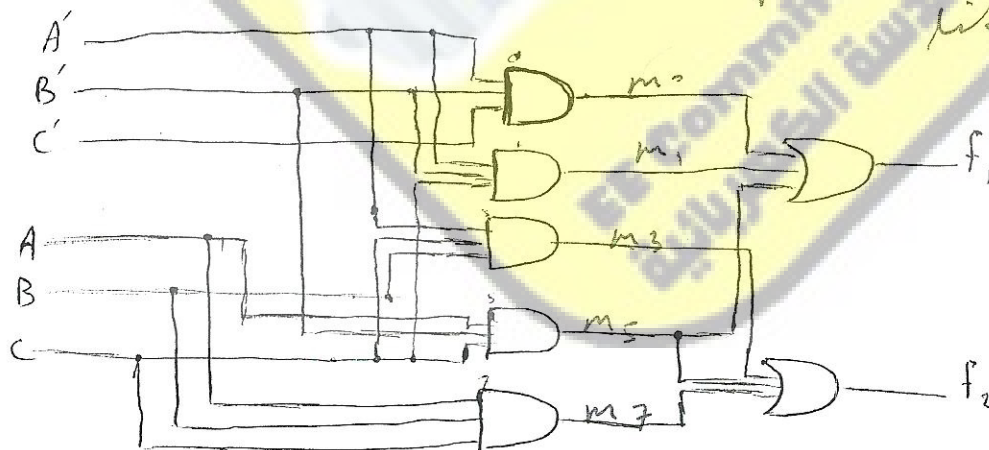
Implement this circuit using the minimum number of gates. Assume that inputs are available in normal and complemented forms.

Hint: Circuit may be implemented using five gates.

$$f_1 = A'B'C' + A'B'C + ABC$$

$$f_2 = A'BC + AB'C + ABC$$

why didn't you simplify?
 too many gates & literals.



$$\begin{array}{r}
 2 \text{ extra gates} \quad -8 \\
 10 = \text{literals} \quad -10 \\
 \hline
 -18
 \end{array}$$